



**General Certificate of Education (A-level)  
January 2012**

**Mathematics**

**MD01**

**(Specification 6360)**

**Decision 1**

**Final**

***Mark Scheme***

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Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all examiners participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for standardisation each examiner analyses a number of students' scripts: alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, examiners encounter unusual answers which have not been raised they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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### Key to mark scheme abbreviations

M	mark is for method
m or dM	mark is dependent on one or more M marks and is for method
A	mark is dependent on M or m marks and is for accuracy
B	mark is independent of M or m marks and is for method and accuracy
E	mark is for explanation
✓ or ft or F	follow through from previous incorrect result
CAO	correct answer only
CSO	correct solution only
AWFW	anything which falls within
AWRT	anything which rounds to
ACF	any correct form
AG	answer given
SC	special case
OE	or equivalent
A2,1	2 or 1 (or 0) accuracy marks
-x EE	deduct x marks for each error
NMS	no method shown
PI	possibly implied
SCA	substantially correct approach
c	candidate
sf	significant figure(s)
dp	decimal place(s)

### No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

**Otherwise we require evidence of a correct method for any marks to be awarded.**

MD01

Q	Solution	Marks	Total	Comments
1	$\begin{array}{cccccccc} 37 & 25 & 16 & 12 & 36 & 24 & 13 & 11 \\ - & \sim & \times & \bullet & - & \sim & \times & \bullet \\ \\ 36 & & & & 37 & & & \\ & 24 & & & & 25 & & \\ & & 13 & & & & 16 & \\ & & & 11 & & & & 12 \\ \\ 36 & 24 & 13 & 11 & 37 & 25 & 16 & 12 \\ - & \times & - & \times & - & \times & - & \times \\ \\ 13 & & 16 & & 36 & & 37 & \\ & 11 & & 12 & & 24 & & 25 \\ \\ 13 & 11 & 16 & 12 & 36 & 24 & 37 & 25 \\ \\ 11 & 12 & 13 & 16 & 24 & 25 & 36 & 37 \end{array}$	M1  A1  m1  A1  A1	5	Using 4 sets of 2  Must see this line  Using 2 sets of 4  Must see this line  All correct
<b>Total</b>			<b>5</b>	
2(a)		M1  A1	2	Bipartite graph, 2 sets of 6 vertices, at least 10 edges  Correct, including labels
(b)	$\left. \begin{array}{l} F \text{ must be with } 6 \\ \therefore E \text{ must be with } 5 \end{array} \right\}$ $\therefore B \text{ must be with } 2$ $\therefore A \text{ \& } C \text{ both with } 1$ <p>Impossible as two people cannot be allocated to the same task</p>	E1  E1  E1	3	Include conclusion  Or E1 3 must be with $D$ (generous) E1 4 “ “ “ $D$ (generous) E1 Impossible as $D$ cannot do both 3 and 4 (strict)
<b>Total</b>			<b>5</b>	

MD01 (cont)

Q	Solution	Marks	Total	Comments
3(a)	$\left. \begin{array}{l} ED = 6 \\ AC = 8 \\ AD = 10 \\ \text{or} \\ DC = 10 \\ FG = 11 \\ BE = 12 \\ CF = 16 \end{array} \right\}$	M1  A1  A1 B1 A1	5	Kruskal, must have first 2 edges correct & no cycles (edges <b>not</b> lengths must be seen)  AD or CD third edge  BE 5th edge 6 edges All correct
(b)	63	B1	1	
(c)		M1  A1  A1	3	Spanning tree with 5+ edges  Correct including labelling  Correct including labelling on a separate diagram
<b>Total</b>			<b>9</b>	
4(a)	$\left. \begin{array}{l} CE + KH = (35 + 24) = 59 \\ CK + EH = (25 + 40) = 65 \\ CH + EK = (25 + 30) = 55 \end{array} \right\}$ Total = 224 + 55 PI by their '279' = 279	M1 A2,1  M1 A1	5	These 3 correct sets of pairs 3 correct totals, 2 correct totals  224 + their smallest of three pair totals CSO including totals seen
(b)	3	B1	1	
<b>Total</b>			<b>6</b>	

MD01 (cont)

Q	Solution	Marks	Total	Comments
5(a)		<p>B1 B1 B1</p> <p>M1</p> <p>A1</p> <p>B1</p>	6	<p>Each line must be straight to have the B mark available. For all lines, must be correct to ½ square horizontal and vertical at the indicated vertices.</p> <p><math>y = 20</math> line through (4,40) and (16,10) line through (0,25) and (10,15)</p> <p>any line through origin (or if extended, through the origin) with positive gradient (generous ± 1 square at the origin)</p> <p>lines through (10,20) <b>and</b> (10,40) as well as origin (normal accuracy rules)</p> <p>FR, all lines correct and region labelled (condone no shading, ignore 'poor' shading)</p>
(b)(i)	<p>(Min at) <math>x = 5, y = 20</math> (P =) 45</p>	<p>B1 B1</p>		<p>Accept (5, 20)</p>
(ii)	<p>(Min at) <math>x = 10, y = 20</math> (P =) 10</p>	<p>B1 B1</p>	4	<p>Accept (10, 20)</p>
<b>Total</b>			<b>10</b>	

MD01 (cont)

Q	Solution	Marks	Total	Comments
6(a)		<p>M1</p> <p>A1</p> <p>m1</p> <p>m1</p> <p>m1</p> <p>A1</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>B1</p>	<p>7</p> <p>1</p> <p>3</p>	<p>SCA, 2 values at <i>C</i> or <i>D</i></p> <p>Correct values at <i>D</i></p> <p>4 values at <i>F</i></p> <p>2 values at <i>G</i> or <i>H</i></p> <p>2 values at <i>I</i></p> <p>Each m1 depends only on the M1</p> <p>All correct, condone 0 missing at <i>A</i>, with rejected values crossed and final values boxed and no extra values at other vertices.</p> <p>145 at <i>J</i></p> <p>Or reverse</p> <p>or replace their <i>BG</i> in terms of letters or numbers eg <math>55 + 8 + 10 = 73</math>, then 'their 73' - 10 = ...</p> <p>or <math>BG = AG - 10 - 28</math> eg <math>BG = \text{'their 101'} - 10 - 28</math></p> <p>Note: 63 with no working seen scores 2/2</p> <p>Or reverse</p>
(b)	Route: $A B E F G H I J$	B1	1	Or reverse
(c)	<p>'their 135' - (28 + <math>GJ</math>)</p> <p><math>GJ</math> may be in terms of letters or numbers</p> <p>= 63</p> <p>Route: <math>A B G H I J</math></p>	M1	3	Or reverse
<b>Total</b>			<b>11</b>	

MD01 (cont)

Q	Solution	Marks	Total	Comments																																																																
7(a)	<table style="border-collapse: collapse; margin-left: 20px;"> <tr> <td></td> <td style="border-right: 1px solid black; border-bottom: 1px solid black;">A</td> <td style="border-right: 1px solid black; border-bottom: 1px solid black;">B</td> <td style="border-right: 1px solid black; border-bottom: 1px solid black;">C</td> <td style="border-right: 1px solid black; border-bottom: 1px solid black;">D</td> <td style="border-right: 1px solid black; border-bottom: 1px solid black;">E</td> <td style="border-bottom: 1px solid black;">F</td> <td style="border-bottom: 1px solid black;">G</td> </tr> <tr> <td>A</td> <td></td> <td></td> <td></td> <td></td> <td style="border-right: 1px solid black;">8</td> <td></td> <td></td> </tr> <tr> <td>B</td> <td></td> <td></td> <td></td> <td></td> <td style="border-right: 1px solid black;">7</td> <td></td> <td></td> </tr> <tr> <td>C</td> <td></td> <td></td> <td></td> <td></td> <td style="border-right: 1px solid black;">13</td> <td></td> <td></td> </tr> <tr> <td>D</td> <td></td> <td></td> <td></td> <td></td> <td style="border-right: 1px solid black;">4</td> <td></td> <td></td> </tr> <tr> <td>E</td> <td style="border-right: 1px solid black;">8</td> <td style="border-right: 1px solid black;">7</td> <td style="border-right: 1px solid black;">13</td> <td style="border-right: 1px solid black;">4</td> <td style="border-right: 1px solid black;">-</td> <td>10</td> <td>19</td> </tr> <tr> <td>F</td> <td></td> <td></td> <td></td> <td></td> <td style="border-right: 1px solid black;">10</td> <td></td> <td></td> </tr> <tr> <td>G</td> <td></td> <td></td> <td></td> <td></td> <td style="border-right: 1px solid black;">19</td> <td></td> <td></td> </tr> </table>		A	B	C	D	E	F	G	A					8			B					7			C					13			D					4			E	8	7	13	4	-	10	19	F					10			G					19			B1 B1	2	5 correct values in an E 'line' All correct
	A	B	C	D	E	F	G																																																													
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(b)(i)	BADEFGCB	M1 A1 A1		Tour visiting at least 6 vertices Visits all 7 vertices Correct order from B																																																																
	80	B1	4																																																																	
(ii)	B A D E F G <u>E</u> C <u>A</u> B	M1 A1	2	Expansion of GC or CB Both correct																																																																
(iii)	76	B1F	1	Minimum of 76 and their (b)(i)																																																																
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	1	2	4	3	5	6																																																														
	A	B	C	D	F	G																																																														
A	<del>-</del>	<del>2</del>	<del>6</del>	<del>4</del>	<del>16</del>	<del>27</del>																																																														
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(ii)	43 43 + (4 + 7) = 54	B1 M1 A1	3	For 43 seen, or for 2 + 6 + 3 + 12 + 20 Their 43 + 2 different edges from E SC 54 with no working 2/3																																																																
(iii)	64	B1	1																																																																	
(d)	$64 \leq T \leq 76$	B1B1	2	Must be written in symbols																																																																
<b>Total</b>			<b>19</b>																																																																	



MD01 (cont)

Q	Solution	Marks	Total	Comments
8(a)	$\left. \begin{array}{l} 2x+3 > 0 \\ 3x-5 > 0 \\ x+1 > 0 \\ 4x-13 > 0 \end{array} \right\}$ $\left. \begin{array}{l} x > \frac{13}{4} \text{ or } \geq \frac{14}{4} \\ \text{(Integer) so } x \geq 4 \end{array} \right]$	M1		Any of these seen
		A1	2	Candidates may use $\geq 1$ instead of $> 0$ Must see both lines. Ignore further work on other inequalities. Accept 4.6 or 4.7 AWRT
(b)(i)	$\begin{array}{l} 2x+3 > 3x-5 \\ > x+1 \\ > 4x-13 \end{array}$	M1		Any correct ISW, condone use of $\geq$
		A1		2nd correct ISW
		A1	3	All correct ISW
(ii)	$\begin{array}{l} 3x-5 > x+1 \\ > 4x-13 \end{array}$	M1		Either correct ISW, condone use of $\geq$
		A1	2	Both correct ISW
(iii)	$x+1 > 4x-13$	B1	1	ISW
(c)	$\frac{13}{4} < x < \frac{14}{3}$ $x = 4$	M1		Or $4 \leq x < \frac{14}{3}$ , condone $3 < x < \frac{14}{3}$
		A1	2	(Ignore all other inequalities) Must have scored 9/9 earlier SC $x < \frac{14}{3} \therefore x = 4 \quad 1/2$
<b>Total</b>			<b>10</b>	
<b>TOTAL</b>			<b>75</b>	